

**CHAPTER 49****PORTFOLIO RISK AND RETURN  
PART I**

1. (C) **their rates of return tend to change in the same direction.**

**Explanation**

For two stocks with positive covariance, their prices will tend to move together over time and they will tend to produce rates of return greater than their mean returns at the same time and produce rates of return less than their mean returns at the same time.

Positive covariance does not necessarily imply strong positive correlation. Two stocks need not be in the same industry to have a positive covariance.

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

2. (A) **capital allocation line.**

**Explanation**

The line that represents possible combinations of a risky asset and the risk-free asset is referred to as a capital allocation line (CAL). The capital market line (CML) represents possible combinations of the market portfolio with the risk-free asset. A characteristic line is the best fitting linear relationship between excess returns on an asset and excess returns on the market and is used to estimate an asset's beta.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

3. (B) **Portfolio B.**

**Explanation**

Portfolio B is inefficient (falls below the efficient frontier) because for the same risk level (8.7%), you could have portfolio C with a higher expected return (15.1% versus 14.2%).

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

4. (B) 18.7%.

**Explanation**

$HPY = (1,020 + 30 + 30 - 910) / 910 = 0.1868$  or 18.7%.

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

5. (C) A and B.

**Explanation**

Portfolios A and B have the lowest correlation coefficient and will thus create the lowest-risk portfolio.

The standard deviation of a portfolio =  $[W_1^2\sigma_1^2 + W_2^2\sigma_2^2 + 2W_1W_2\sigma_1\sigma_2r_{1,2}]^{1/2}$

The correlation coefficient,  $r_{1,2}$ , varies from + 1 to - 1. The smaller the correlation coefficient, the smaller the portfolio can be. If the correlation coefficient were - 1, it would be possible to make the portfolio go to zero by picking the proper weightings of  $W_1$  and  $W_2$ .

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

6. (A) level of risk aversion in the market.

**Explanation**

The level of risk aversion in the market is not a required input. The model requires that investors know the expected return and variance of each security as well as the covariance between all securities.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

7. (A) risk averse.

**Explanation**

Given two investments with the same expected return, a risk averse investor will prefer the investment with less risk. A risk neutral investor will be indifferent between the two investments. A risk seeking investor will prefer the investment with more risk.

(Study Session 17, Module 49.2, LOS 49.e)

**Related Material**

[SchweserNotes - Book 5](#)

8. (A) more risk averse than Jones and will choose an optimal portfolio with a lower expected return.

**Explanation**

Steeply sloped risk-return indifference curves indicate that a greater increase in expected return is required as compensation for assuming an additional unit of risk, compared to less-steep indifference curves. The more risk-averse Smith will choose an optimal portfolio with lower risk and a lower expected return than the less risk-averse Jones's optimal portfolio.

**For Further Reference:**

(Study Session 17, Module 49.3, LOS 49.i)

CFA® Program Curriculum, Volume 5, page 473

**Related Material**

[SchweserNotes - Book 5](#)

- 9 (B) 0.94%.

**Explanation**

Using the financial calculator, the initial investment ( $CF_0$ ) is -100,000. The income is +5,000 ( $CF_1$ ), and the contribution is -25,000 ( $CF_2$ ). Finally, the ending value is +123,000 ( $CF_3$ ) available to the investor. Compute IRR = 0.94

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

10. (B) 10.4%.

**Explanation**

January - March return =  $51,000 / 50,000 - 1 = 2.00\%$

April - June return =  $60,000 / (51,000 + 10,000) - 1 = -1.64\%$

July - December return =  $33,000 / (60,000 - 30,000) - 1 = 10.00\%$

Time-weighted return =  $[(1 + 0.02)(1 - 0.0164)(1 + 0.10)] - 1 = 0.1036$  or 10.36%

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

11. (A) B.

**Explanation**

Portfolio B is not on the efficient frontier because it has a lower return, but higher risk, than Portfolio D.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

12. (B) are not affected by the timing of cash flows.

**Explanation**

Time-weighted returns are not affected by the timing of cash flows. Money-weighted returns, by contrast, will be higher when funds are added at a favorable investment period or will be lower when funds are added during an unfavorable period. Thus, time-weighted returns offer a better performance measure because they are not affected by the timing of flows into and out of the account.

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

13. (B) money-weighted rate of return will tend to be elevated.

**Explanation**

The time-weighted returns are what they are and will not be affected by cash inflows or outflows. The money-weighted return is susceptible to distortions resulting from cash inflows and outflows. The money-weighted return will be biased upward if the funds are invested just prior to a period of favorable performance and will be biased downward if funds are invested just prior to a period of relatively unfavorable performance. The opposite will be true for cash outflows.

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

14. (B) 100% 0%

**Explanation**

Because there is a perfectly positive correlation, there is no benefit to diversification. Therefore, the investor should put all his money into Stock A (with the lowest standard deviation) to minimize the risk (standard deviation) of the portfolio.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

15. (B) Real return.

**Explanation**

No calculations are needed. The real return is greater than the nominal return because the inflation rate is negative. The leveraged return is more negative than the nominal return because the investment lost value and leverage magnifies the loss.

**For Further Reference:**

(Study Session 17, Module 49.1, LOS 49.a)  
CFA® Program Curriculum, Volume 5, page 442

**Related Material**

[SchweserNotes - Book 5](#)

16. (B) 0.00724.

**Explanation**

$$0.8^2(0.0081) + 0.2^2(0.07^2) + 2(0.8)(0.2)(0.0058) = 0.00724.$$

**For Further Reference:**

(Study Session 17, Module 49.3, LOS 49.f)  
CFA® Program Curriculum, Volume 5, page 476

**Related Material**

[SchweserNotes - Book 5](#)

17. (A) 0.06%.

**Explanation**

The holding period return in year one is  $(\$89.00 - \$100.00 + \$1.00) / \$100.00 = -10.00\%$ .

The holding period return in year two is  $(\$98.00 - \$89.00 + \$1.00) / \$89 = 11.24\%$ .

The time-weighted return is  $[(1 + (-0.1000))(1 + 0.1124)]^{1/2} - 1 = 0.06\%$ .

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

18. (C) 0.05830.

**Explanation**

$COVA_{A,B} = (r_{A,B})(SD_A)(SD_B)$ , where  $r$  = correlation coefficient and  $SD_x$  = standard deviation of stock  $x$

$$\text{Then, } (r_{A,B}) = COVA_{A,B} / (SD_A \times SD_B) = 0.007 / (0.400 \times 0.300) = 0.0583$$

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

19. (B) 18.4%.

**Explanation**

The expected standard deviation of portfolio returns is:

$$[0.40^2 \times 0.15^2 + 0.60^2 \times 0.25^2 + 2(0.40 \times 0.60 \times 0.0158)]^{1/2} = 18.35\%.$$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

20. (A) investor's highest utility curve is tangent to the efficient frontier.

**Explanation**

The optimal portfolio for an investor is determined as the point where the investor's highest utility curve is tangent to the efficient frontier.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

21. (B) 51.4%.

**Explanation**

To calculate the time-weighted return:

**Step 1:** Separate the time periods into holding periods and calculate the return over that period:

Holding period 1:  $P_0 = \$50.00$

$D_1 = \$5.00$

$P_1 = \$75.00$  (from information on second stock purchase)

$HPR_1 = (75 - 50 + 5) / 50 = 0.60$ , or 60%

Holding period 2:  $P_1 = \$75.00$

$D_2 = \$7.50$

$P_2 = \$100.00$

$HPR_2 = (100 - 75 + 7.50) / 75 = 0.433$ , or 43.3%.

**Step 2:** Use the geometric mean to calculate the return over both periods

Return =  $[(1 + HPR_1) \times (1 + HPR_2)]^{1/2} - 1 = [(1.60) \times (1.433)]^{1/2} - 1 = 0.5142$ , or **51.4%**.

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

22. (B) B, C, and F.

**Explanation**

Portfolio B cannot lie on the frontier because its risk is higher than that of Portfolio A's with lower return. Portfolio C cannot lie on the frontier because it has higher risk than Portfolio D with lower return. Portfolio F cannot lie on the frontier because its risk is higher than Portfolio D.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

23. (A) **Portfolio C.**

**Explanation**

Portfolio C cannot lie on the frontier because it has the same return as Portfolio D, but has more risk.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

24. (C) **When the return on an asset added to a portfolio has a correlation coefficient of less than one with the other portfolio asset returns but has the same risk, adding the asset will not decrease the overall portfolio standard deviation.**

**Explanation**

When the return on an asset added to a portfolio has a correlation coefficient of less than one with the other portfolio asset returns but has the same risk, adding the asset will decrease the overall portfolio standard deviation. Any time the correlation coefficient is less than one, there are benefits from diversification. The other choices are true.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

25. (A) **-100.00.**

**Explanation**

Covariance = correlation coefficient x standard deviation<sub>stock1</sub> x standard deviation<sub>stock2</sub> = (-1.00) (10.00)(10.00) = -100.00.

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

26. (C) **6.35%.**

**Explanation**

T = 0: Purchase of first share = -\$100.00

T = 1: Dividend from first share = +\$1.00

Purchase of 3 more shares = -\$267.00

T = 2: Dividend from four shares = +4.00

Proceeds from selling shares = +\$392.00

The money-weighted return is the rate that solves the equation:

$$\$100.00 = -\$266.00 / (1 + r) + 396.00 / (1 + r)^2.$$

CFO = -100; CF1 = -266; CF2 = 396; CPT → IRR = 6.35%.

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

27. (A) 0.5795.

**Explanation**

The portfolio standard deviation =  $[(0.4)^2(0.25) + (0.6)^2(0.4) + 2(0.4)(0.6)1(0.25)^{0.5}(0.4)^{0.5}]^{0.5} = 0.5795$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

28. (B) the global minimum variance portfolio.

**Explanation**

According to the CAPM, rational, risk-averse investors will optimally choose to hold a portfolio along the capital market line. This can range from a 100% allocation to the risk-free asset to a leveraged position in the market portfolio constructed by borrowing at the risk-free rate to invest more than 100% of the portfolio equity value in the market portfolio. The global minimum variance portfolio lies below the CML and is not an efficient portfolio under the assumptions of the CAPM.

**For Further Reference:**

(Study Session 17, Module 49.3, LOS 49.h)

CFA® Program Curriculum, Volume 5, page 491

**Related Material**

[SchweserNotes - Book 5](#)

29. (C) Treasury bills.

**Explanation**

Based on data for securities in the United States from 1926 to 2008, Treasury bills exhibited a lower standard deviation of monthly returns than both large-cap stocks and long-term corporate bonds.

(Study Session 17, Module 49.1, LOS 49.c)

**Related Material**

[SchweserNotes - Book 5](#)

30. (A) higher average annual returns and higher standard deviation of returns.

**Explanation**

Based on data for securities in the United States from 1926 to 2008, both small-cap stocks and large-cap stocks have exhibited higher average annual returns and higher standard deviations of returns than long-term corporate bonds and long-term government bonds. Results over long periods of time have been similar in other developed markets.

(Study Session 17, Module 49.1, LOS 49.c)

**Related Material**

[SchweserNotes - Book 5](#)

**31. (B) higher rates of return.**

**Explanation**

Investors are risk averse. Given a choice between two assets with equal rates of return, the investor will always select the asset with the lowest level of risk. This means that there is a positive relationship between expected returns (ER) and expected risk ( $E\sigma$ ) and the risk return line (capital market line [CML] and security market line [SML]) is upward sweeping.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

**32. (B) highest utility.**

**Explanation**

The optimal portfolio in the Markowitz framework occurs when the investor achieves the diversified portfolio with the highest utility.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

**33. (B) If the covariance is negative, the rates of return on two investments will always move in different directions relative to their means.**

**Explanation**

Negative covariance means rates of return for one security will tend to be above its mean return in periods when the other is below its mean return, and vice versa. Positive covariance means that returns on both securities will tend to be above (or below) their mean returns in the same time periods. For the returns to always move in opposite directions, they would have to be perfectly negatively correlated. Negative covariance by itself does not imply anything about the strength of the negative correlation, it must be standardized by dividing by the product of the securities' standard deviations of return.

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

**34. (A) beta.**

**Explanation**

Beta is not an input to calculate the variance of a two-asset portfolio. The formula for calculating the variance of a two-asset portfolio is:

$$\sigma_P^2 = w_A^2 \sigma_A^2 + w_B^2 \sigma_B^2 + 2w_A w_B \text{Cov}_{AB}$$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

35. (B) 6.

**Explanation**

The formula for the covariance for historical data is:

$$\text{cov}_{1,2} = \{\sum[(R_{\text{stock A}} - \text{Mean } R_A)(R_{\text{stock B}} - \text{Mean } R_B)]\} / (n - 1)$$

$$\text{Mean } R_A = (10 + 6 + 8) / 3 = 8, \text{ Mean } R_B = (15 + 9 + 12) / 3 = 12$$

$$\text{Here, } \text{cov}_{1,2} = [(10 - 8)(15 - 12) + (6 - 8)(9 - 12) + (8 - 8)(12 - 12)] / 2 = 6$$

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

36. (A) 0.0007.

**Explanation**

The variance of the portfolio is found by:

$$[W_1^2\sigma_1^2 + W_2^2\sigma_2^2 + 2W_1W_2\sigma_1\sigma_2r_{1,2}], \text{ or } [(0.15)^2(0.0071) + (0.85)^2(0.0008) + (2)(0.15)(0.85)(0.0843)(0.0283)(-0.04)] = 0.0007.$$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

37. (C) 0.0375.

**Explanation**

$\text{Cov}_{X,Y} = (r_{X,Y})(s_X)(s_Y)$ , where  $r$  = correlation coefficient,  $s_x$  = standard deviation of stock X, and  $s_y$  = standard deviation of stock Y

$$\text{Then, } (r_{X,Y}) = \text{Cov}_{X,Y} / (\text{SD}_X \times \text{SD}_Y) = 0.009 / (0.600 \times 0.400) = 0.0375$$

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

38. (B) 23.44%.

**Explanation**

$$\text{HPR} = [\text{ending value} - \text{beginning value}] / \text{beginning value}$$

$$\text{HPR} = [(2 + 37.50) - 32] / 32 = 0.2344.$$

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

39. (A) money-weighted return.

**Explanation**

The money-weighted return is the internal rate of return on a portfolio that equates the present value of inflows and outflows over a period of time.

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

40. (C) the set of portfolios that dominate all others as to risk and return.

**Explanation**

The efficient set is the set of portfolios that dominate all other portfolios as to risk and return. That is, they have highest expected return at each level of risk.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

41. (A) greater.

**Explanation**

Perfect positive correlation ( $r = +1$ ) of the returns of two assets offers no risk reduction, whereas perfect negative correlation ( $r = -1$ ) offers the greatest risk reduction.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

42. (B) -0.80.

**Explanation**

Correlation = (covariance of X and Y) / [(standard deviation of X)(standard deviation of Y)] =  $-0.0031 / [(0.072)(0.054)] = -0.797$ .

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

43. (B) if they have the same expected return.

**Explanation**

Investors are risk averse. Given a choice between assets with equal rates of expected return, the investor will always select the asset with the lowest level of risk. Risk aversion does not imply that an investor will choose the less risky of two assets in all cases, or that an investor is unwilling to accept greater risk to achieve a greater expected return.

(Study Session 17, Module 49.2, LOS 49.e)

**Related Material**

[SchweserNotes - Book 5](#)

44. (A) 48.9%.

**Explanation**

To determine the money weighted rate of return, use your calculator's cash flow and IRR functions. The cash flows are as follows:

CF<sup>0</sup>: initial cash outflow for purchase = \$50

CF1: dividend inflow of \$5 - cash outflow for additional purchase of \$75 = net cash outflow of -\$70

CF2: dividend inflow (2 x \$7.50 = \$15) + cash inflow from sale (2 x \$100 = \$200) = net cash inflow of \$215

Enter the cash flows and compute IRR:

CFO = -50; CF1 = -70; CF2 = +215; CPT IRR = 48.8607 (Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

45. (A) 0.25.

**Explanation**

The formula for the variance of a 2-stock portfolio is:

$$s^2 = [W_A^2\sigma_A^2 + W_B^2\sigma_B^2 + 2W_AW_B\sigma_A\sigma_Br_{A,B}]$$

Since  $\sigma_A\sigma_Br_{A,B} = \text{Cov}_{A,B}$ , then

$$s^2 = [(0.72 \times 0.55^2) + (0.3^2 \times 0.85^2) + (2 \times 0.7 \times 0.3 \times 0.09)] = [0.1482 + 0.0650 + 0.0378] = 0.2511.$$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

46. (A) the correlation coefficient between the assets is less than 1.

**Explanation**

There are benefits to diversification as long as the correlation coefficient between the assets is less than 1.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

47. (B) If the correlation coefficient were 0, a zero variance portfolio could be constructed.

**Explanation**

A correlation coefficient of zero means that there is no relationship between the stock's returns. The other statements are true.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

**48. (A) 100% in Stock B.****Explanation**

Since the stocks are perfectly correlated, there is no benefit from diversification. So, invest in the stock with the lowest risk.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

**49. (B) +1.00.****Explanation**

Adding any stock that is not perfectly correlated with the portfolio (+1) will reduce the risk of the portfolio.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

**50. (A) Jones or Lewis, but not Kelly.****Explanation**

Risk aversion means that to accept greater risk, an investor must be compensated with a higher expected return. A risk-averse investor will not select a portfolio if another portfolio offers a higher expected return with the same risk, or lower risk with the same expected return. Thus a rational investor would always choose Lewis over Kelly, because Lewis has both a higher expected return and lower risk than Kelly. Neither Lewis nor Kelly is necessarily preferable to Jones, because although Jones has a lower expected return, it also has lower risk. Therefore, either Jones or Lewis might be selected by a rational investor, but Kelly would not be.

(Study Session 17, Module 49.2, LOS 49.e)

**Related Material**

[SchweserNotes - Book 5](#)

**51. (B) Portfolio X.****Explanation**

Portfolio X has a lower expected return and a higher standard deviation than Portfolio Y. X must be inefficient.

**For Further Reference:**

(Study Session 17, Module 49.3, LOS 49.h)

CFA® Program Curriculum, Volume 5, page 491

**Related Material**

[SchweserNotes - Book 5](#)

52. (B) 0.0264.

**Explanation**

$\text{cov}_{1,2} = 0.75 \times 0.16 \times 0.22 = 0.0264 = \text{covariance between A and B.}$

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

53. (B) geometric mean return.

**Explanation**

Geometric mean return (time-weighted return) is the most appropriate method for performance measurement as it does not consider additions to or withdrawals from the account.

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

54. (A) Z.

**Explanation**

Portfolio Z must be inefficient because its risk is higher than Portfolio Y and its expected return is lower than Portfolio Y.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

55. (C) fees.

**Explanation**

The net return on a portfolio is its gross return minus management and administrative fees. A return adjusted for taxes is called an after-tax return. A return adjusted for inflation is called a real return.

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

56. (A) the highest expected return for any given level of risk.

**Explanation**

The efficient frontier is the set of efficient portfolios that gives investors the highest expected return for any given level of risk, or the lowest risk for any given level of expected return. Efficient portfolios have low diversification ratios.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

57. (B) 0.40.

**Explanation**

$COV_{A,B} = (r_{A,B})(SD_A)(SD_B)$ , where  $r$  = correlation coefficient and  $SD_x$  = standard deviation of stock  $x$

Then,  $(r_{A,B}) = COV_{A,B} / (SD_A \times SD_B) = 0.008 / (0.100 \times 0.200) = 0.40$

**Remember:** The correlation coefficient must be between -1 and 1.

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

58. (B) 1.5%.

**Explanation**

$HPY = [(interest + ending\ value) / beginning\ value] - 1$

$= [(100 + 915) / 1,000] - 1$

$= 1.015 - 1 = 1.5\%$

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

59. (A) decrease.

**Explanation**

$P_{1,2} = 0.048 / (0.026^{0.5} \times 0.18^{0.5}) = 0.69$  which is lower than the original 0.79.

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

60. (B) geometric mean return.

**Explanation**

Geometric Mean Return =  $\sqrt[3]{(1 + 0.06)(1 - 0.37)(1 + 0.27)} - 1 = -5.34\%$

Holding period return =  $(1 + 0.06)(1 - 0.37)(1 + 0.27) - 1 = -15.2\%$

Arithmetic mean return =  $(6\% - 37\% + 27\%) / 3 = -1.33\%$ .

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

61. (C) is the portfolio that gives the investor the maximum level of return.

**Explanation**

This statement is incorrect because it does not specify that risk must also be considered. (Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

62. (B) decrease.

**Explanation**

If the correlation coefficient is less than 1, there are benefits to diversification. Thus, adding the stock will reduce the portfolio's standard deviation.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

63. (A) more if she bought Branton Co.

**Explanation**

In portfolio composition questions, return and standard deviation are the key variables. Here you are told that both returns and standard deviations are equal. Thus, you just want to pick the companies with the lowest covariance, because that would mean you picked the ones with the lowest correlation coefficient.

$$\sigma_{\text{portfolio}} = [W_1^2 \sigma_1^2 + W_2^2 \sigma_2^2 + 2W_1 W_2 \sigma_1 \sigma_2 r_{1,2}]^{1/2} \text{ where } \sigma_{\text{Randy}} = Y_{\text{Branton}} = \sigma_{\text{XYZ}}$$

so you want to pick the lowest covariance which is between Randy and Branton.

(Study Session 17, Module 49.3, LOS 49.g)

**Related Material**

[SchweserNotes - Book 5](#)

64. (A) variance of returns.

**Explanation**

The Markowitz framework assumes that all investors view risk as the variability of returns. The variability of returns is measured as the variance (or equivalently standard deviation) of returns. The capital asset pricing model (CAPM) employs beta as the measure of an investment's systematic risk.

**For Further Reference:**

(Study Session 17, Module 49.3, LOS 49.h)

CFA® Program Curriculum, Volume 5, page 491

**Related Material**

[SchweserNotes - Book 5](#)

65. (C) The frontier extends to the left, or northwest quadrant representing a reduction in risk while maintaining or enhancing portfolio returns.

**Explanation**

Reducing correlation between the two assets results in the efficient frontier expanding to the left and possibly slightly upward. This reflects the influence of correlation on reducing portfolio risk.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

66. (A) 27.5%.

**Explanation**

HPR = [ending value - beginning value] / beginning value  
 = (75 + 1.50 - 60) / 60 = 27.5%.

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

67. (C) There is a portfolio that has a lower risk for the same return.

**Explanation**

The efficient frontier outlines the set of portfolios that gives investors the highest return for a given level of risk or the lowest risk for a given level of return. Therefore, if a portfolio is not on the efficient frontier, there must be a portfolio that has lower risk for the same return. Equivalently, there must be a portfolio that produces a higher return for the same risk.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

68. (A) 10.8%; 9.4%.

**Explanation**

Time-weighted return =  $(225 + 5 - 200) / 200 = 15\%$ ;  $(470 + 10 - 450) / 450 = 6.67\%$ ;  $[(1.15)(1.0667)]^{1/2} - 1 = 10.8\%$

Money-weighted return:  $200 + [225 / (1 + \text{return})] = [5 / (1 + \text{return})] + [480 / (1 + \text{return})^2]$ ; money return = approximately 9.4%

Note that the easiest way to solve for the money-weighted return is to set up the equation and **plug in the answer choices** to find the discount rate that makes outflows equal to inflows.

Using the financial calculators to calculate the money-weighted return: (The following keystrokes assume that the financial memory registers are cleared of prior work.)

TI Business Analyst II Plus®

- Enter CF<sub>0</sub>: 200, +/-, Enter, down arrow
- Enter CF<sub>1</sub>: 220, +/-, Enter, down arrow, down arrow
- Enter CF<sub>2</sub>: 480, Enter, down arrow, down arrow,
- Compute IRR: IRR, CPT
- Result: 9.39

HP 12C®

- Enter CF<sub>0</sub>: 200, CHS, g, CF<sub>0</sub>
- Enter CF<sub>1</sub>: 220, CHS, g, CF<sub>j</sub>
- Enter CF<sub>2</sub>: 480, g, CF<sub>j</sub>

- Compute IRR: f, IRR
- Result: 9.39

(Study Session 17, Module 49.1, LOS 49.b)

**Related Material**

[SchweserNotes - Book 5](#)

- 69. (B) Variance = 0.03836; Standard Deviation = 19.59%.**

**Explanation**

$$(0.40)^2(0.18)^2 + (0.60)^2(0.24)^2 + 2(0.4)(0.6)(0.18)(0.24)(0.6) = 0.03836.$$

$$0.03836^{0.5} = 0.1959 \text{ or } 19.59\%.$$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

- 70. (C) 31.25%.**

**Explanation**

Return = [dividend + (ending value - beginning value)] / beginning price value

$$= [1.25 + (25 - 20)] / 20 = 6.25 / 20 = 0.3125$$

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

- 71. (C) real return.**

**Explanation**

A real return is adjusted for the effects of inflation and is used to measure the increase in purchasing power over time.

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

- 72. (C) Investor X is less risk-averse than Investor Y.**

**Explanation**

Investor X has a steep indifference curve, indicating that he is risk-averse. Flatter indifference curves, such as those for Investor Y, indicate a less risk-averse investor. The other choices are true. A more risk-averse investor will likely obtain lower returns than a less risk-averse investor.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

**73. (C) the individual's utility curve.**

**Explanation**

The optimal portfolio for each investor is the highest indifference curve that is tangent to the efficient frontier. The optimal portfolio is the portfolio that gives the investor the greatest possible utility.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

**74. (C) The slope of the efficient frontier increases steadily risk increases.**

**Explanation**

The slope of the efficient frontier decreases steadily as risk and return increase.

The efficient frontier is the set of portfolios with the greatest expected return for a given level of risk as measured by standard deviation of returns. That is, for a given level of risk, an expected return greater than that of the portfolio on the efficient frontier is not attainable, and a portfolio with a lower expected return is inefficient.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

**75. (B) +1.**

**Explanation**

The formula is:  $\text{Covariance of A and B} / [(\text{Standard deviation of A})(\text{Standard Deviation of B})] = (\text{Correlation Coefficient of A and B}) = (0.015476) / [(0.106)(0.146)] = 1.$

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

**76. (A) 100% in Bridgeport.**

**Explanation**

First, calculate the correlation coefficient to check whether diversification will provide any benefit.

$$r_{\text{Bridgeport, Rockaway}} = \text{COV}_{\text{Bridgeport, Rockaway}} / [(\sigma_{\text{Bridgeport}}) \times (\sigma_{\text{Rockaway}})] = 0.0325 / (0.13 \times 0.25) = 1.00$$

Since the stocks are perfectly positively correlated, there are no diversification benefits and we select the stock with the lowest risk (as measured by variance or standard deviation), which is Bridgeport.

(Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

77. (B) 0.370.

**Explanation**

$\sigma$  portfolio =  $[W_1^2\sigma_1^2 + W_2^2\sigma_2^2 + 2W_1W_2\sigma_1\sigma_2r_{1,2}]^{1/2}$  given  $r_{1,2} = +1$

$\sigma = [W_1^2\sigma_1^2 + W_2^2\sigma_2^2 + 2W_1W_2\sigma_1\sigma_2]^{1/2} = (W_1\sigma_1 + W_2\sigma_2)^{1/2}$

$\sigma = (W_1\sigma_1 + W_2\sigma_2) = (0.3)(0.3) + (0.7)(0.4) = 0.09 + 0.28 = 0.37$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

78. (A) Investors will want to invest in the portfolio on the efficient frontier that offers the highest rate of return.

**Explanation**

The optimal portfolio for each investor is the highest indifference curve that is tangent to the efficient frontier.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

79. (A) Flatter.

**Explanation**

Investors who are less risk averse will have flatter indifference curves, meaning they are willing to take on more risk for a slightly higher return. Investors who are more risk averse require a much higher return to accept more risk, producing steeper indifference curves.

(Study Session 17, Module 49.3, LOS 49.i)

**Related Material**

[SchweserNotes - Book 5](#)

80. (A) B.

**Explanation**

Portfolio B has a lower expected return than Portfolio C with a *higher* standard deviation. (Study Session 17, Module 49.3, LOS 49.h)

**Related Material**

[SchweserNotes - Book 5](#)

81. (C) 12.5%.

**Explanation**

The holding period return (HPR) is calculated as follows:

$$\text{HPR} = (P_t - P_{t-1} + D_t) / P_{t-1}$$

where:

$P_t$  = price per share at the end of time period  $t$

$D_t$  = cash distributions received during time period  $t$ .

Here,  $HPR = (850 - 800 + 50) / 800 = 0.1250$ , or **12.50%**.

(Study Session 17, Module 49.1, LOS 49.a)

**Related Material**

[SchweserNotes - Book 5](#)

**82. (B) Fiona's indifference curves are flatter than Scott's.**

**Explanation**

Even risk-averse investors will prefer leveraged risky portfolios if the increase in expected return is enough to offset the increase in portfolio risk. Scott's portfolio selection implies that she is more risk averse than Fiona, has steeper indifference curves, and is willing to take on less additional risk for an incremental increase in expected returns than Fiona.

**For Further Reference:**

(Study Session 17, Module 49.3, LOS 49.i)

CFA® Program Curriculum, Volume 5, page 473

**Related Material**

[SchweserNotes - Book 5](#)

**83. (A) 0.25.**

**Explanation**

The correlation between the two stocks is:

$$\rho_{A,B} = \text{COV}_{A,B} / (\sigma_A \times \sigma_B) = 0.001 / (0.05 \times 0.08) = 0.001 / (0.004) = 0.25$$

Note that the formula uses the standard deviations, not the variances, of the returns on the two securities.

(Study Session 17, Module 49.1, LOS 49.c)

**Related Material**

[SchweserNotes - Book 5](#)

**84. (C) 0.1600.**

**Explanation**

The formula for the standard deviation of a 2-stock portfolio is:

$$\sigma = [W_A^2 \sigma_A^2 + W_B^2 \sigma_B^2 + 2W_A W_B \sigma_A \sigma_B \rho_{A,B}]^{1/2}$$

$$a = [(0.7^2 \times 0.2^2) + (0.3^2 \times 0.15^2) + (2 \times 0.7 \times 0.3 \times 0.2 \times 0.15 \times 0.32)]^{1/2} = [0.0196 + 0.002025 + 0.004032]^{1/2} = 0.0256570^{1/2} = 0.1602, \text{ or approximately } \mathbf{16.0\%}.$$

(Study Session 17, Module 49.3, LOS 49.f)

**Related Material**

[SchweserNotes - Book 5](#)

85. (B) 0.0022.

**Explanation**

The formula is:  $(\text{correlation})(\text{standard deviation of A})(\text{standard deviation of B}) = (0.20)(0.122)(0.089) = 0.0022$ .

(Study Session 17, Module 49.2, LOS 49.d)

**Related Material**

[SchweserNotes - Book 5](#)

86. (B) a positive relationship.

**Explanation**

In most markets and for most asset classes, higher average returns have historically been associated with higher risk (standard deviation of returns).

(Study Session 17, Module 49.1, LOS 49.c)

**Related Material**

[SchweserNotes - Book 5](#)

